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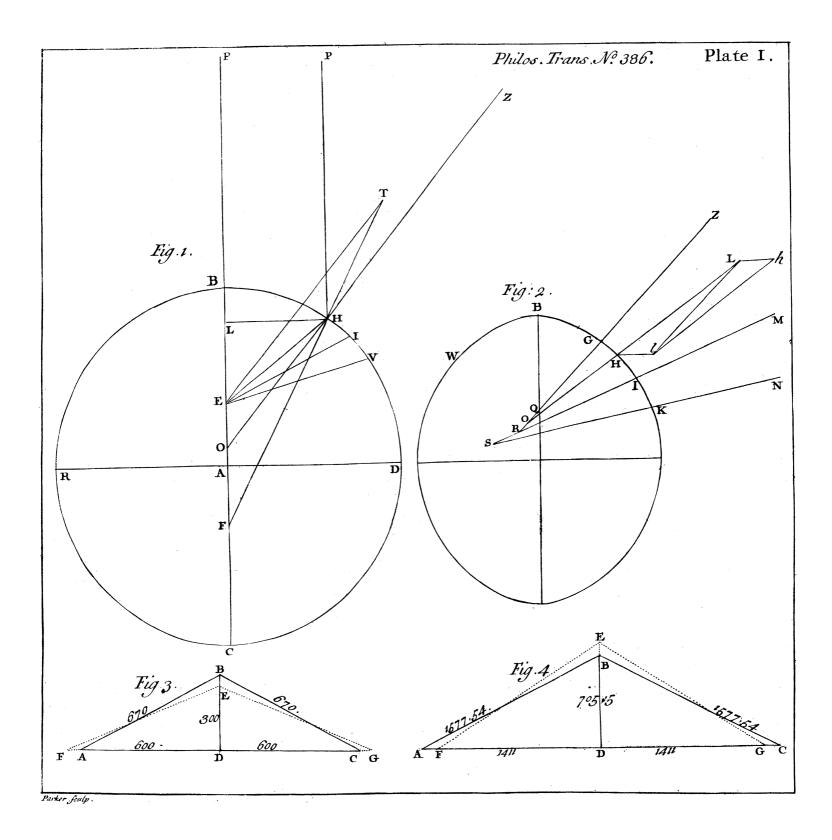
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A Dissertation concerning the Figure of the Earth, by the Reverend John Theophilus Desaguliers, LL. D. F. R. S.

THAT the Earth (that is, our Terraqueous Habitation) is of a spherical Figure, or nearly such, has been prov'd so often, and by so many unanswerable Arguments, that to repeat them here must needs be tedious to this learned Society. But, as a little Variation from a true Sphere (besides the Irregularity of high Hills and deep Vallies) does not hinder us from calling the Earth a Globe; so, to determine what that Variation may be, since modern Philosophers are divided about it, may be a Subject not ungrateful at this Time.

Monsieur Cassini says: "That the Earth is an ob"long Spheroid, higher at the Poles than the Aquator,
"making the Axis longer than a Diameter of the Aqua"tor about thirteen French Leagues, which he deduces from comparing his Father's Measures of the
"Meridian, from Paris to the Pyrenaean Mountains, with those of Monsieur Picard; of which an
"Account may be seen in the Memoirs of the Royal
"Academy for 1713. But having afterwards continued the Meridian, which is drawn through France,
from Paris to Dunkerque, he still draws Consequences to prove the Earth an oblong Spheroid;
but then makes the Axis exceed the Aquatorial
"Diameter 34 Leagues.

" Sir Isaac Newton makes the Earth higher at the " Aguator, and, consequently, flatted towards the "Poles, reckoning its Acquatorial Diameter 34 English " Miles longer than the Axis; which he proves from " the Principles of Gravity, and the Centrifugal Force "that arises from the Diurnal Rotation of the Earth; " and, to confirm this, mentions feveral Experiments " on Pendulums, which have been made shorter, to " fwing Seconds, near the Æquator, than in greater " Latitudes."

These are the two Opinions which have divided Philosophers, and which we propose to examine here.

Monsieur Cassini, taking the Measures above-men tion'd to be exact enough, not only to determine the Magnitude of a Degree of the Earth, corresponding with a Degree of the great Circle of the Heavens, but also to shew the Difference in the Degrees of the Earth; (reckoning those, that were measured in the South of France, to exceed those towards the North, by a certain Number of Toises and Feet) demonstrates, that if the Degrees of the Earth are longer towards the Æquator than the Poles, the Plane of the Meridian must be an Ellipse, whose long Axis is that of the Earth. Here follows his first Demonstration. [See the French Memoirs for the Year 17137

" Let B D C R \* be an Ellipse that represents a " Meridian of the Earth, whose Poles B and C are at " Ends of the great Axis BC, and whose Foci E and

" F are taken at Pleasure. Now, to divide this

" Ellipse into Degrees, that is, to find several "Points H, I, V, such, that the Distance, from the

" Pole to the Zenith, of every one of them, shall

" be of any given Number of Degrees.

<sup>\*</sup> Fig. 1.

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"From E, one of the Foci of the Ellipse, draw the Line E T, so that it may, with the Axis B C, make the Angle B E T equal to the Distance given from the Pole to the Zenith. From the other Focus F, with the Distance B C equal to the Axis, draw an Arc, to cut the Line E T at T. I say, that the Line F T, drawn from the Point T to the Focus F, will cut the Ellipse at the Point H; which Point is such, that the Distance of the Pole, from its Zenith, contains the given Number of Degrees.

## "DEMONSTRATION.

" From the Point H, raise H Z, perpendicular to " the Ellipse which will pass through the Zenith Z; and, being produc'd inwards, will meet the Axis of " the Earth at O, and (by the Property of the Ellipse) " divide the Angle E H F into two equal Parts. From "the Point H, draw likewise H P, parallel to the Axis " B C, and directed to the Pole P, suppos'd at an infi-" nite Distance. The Angle P H Z, or P O Z, mea-" fures the Distance, from the Pole to the Zenith, of " an Inhabitant dwelling upon the Earth at the Point " H. F T is equal to the Axis B C, by Construction; but, by the Property of the Ellipse, B C is equal to " EH plus AF; taking away from both FH, which " is common, EH will remain equal to HT. "Angles ETH, TEH, will therefore be equal, " and, consequently, each of them will be half of the " external Angle EHF; but the Angle EHO is " likewise equal to half of the Angle EHF; there-" fore the Angles T E H, E H O, will be equal to " one another; and, consequently, the Lines E T and "HO will be parallel to one another; and the Angle " P O Z, which measures the Distance from the Pole Gg 2

" to the Zenith of the Point H, will be equal to the "Angle B E T, which was, by Construction, taken

" equal to the given Distance of the Pole from the

" Zenith; which was to be demonstrated.

" Now, if the Proportion of the longest Diameter

- " of the Ellipse B C to EF, the Distance of the Foci,
- be taken at Pleasure, one may by Calculation
- "find all the Points of the Ellipse as H, to deter-

" mine the Degrees by this Analogy.

- " As FT, or BC:
- " Is to EF::

" So is the Sine of the Angle P ET (the given Di-

" stance from the Pole to the Zenith):

"To the Sine of the Angle ETF, or TEH:

" whose Quantity will consequently be known. This "Angle TEH being added to the Angle PET, the

" given Distance from the Pole to the Zenith of the

"Point H, will give the Quantity of the Angle B E H, which a Line drawn from the Focus to H, the Point

" requir'd, makes with the Axis of the Ellipse.

"Then in the Triangle E H F, whose Side E F is

- known, as well as the Angle E H F, which is the Double of the Angle T E H, and the Angle F E H
- " Supplement of the Angle B E H; one shall have the
- "Length of the Side EH, known in Parts of the Axis

" BC.

- "After the same Manner, may be found the Angles BEI, BEV, &c. and the Length of the Lines EI,
- " EV, to determine the Distance, from the Pole to the
- " Zenith, of all the Degrees of the Circumference of
- " the Earth; and in the rectilinear Triangles HEI,
- "IEV, whose Sides HE, EI, EV, are known as
- well as the Angles comprehended between the Sides
- "HE, EI, IE, EV, which are the Differences of the Angles BEH, BEI, BEV, determin'd above;

" one

" one shall find the Length of the Chords H I, I V,

" comprehended between each Degree.

Monf. Cassini, in the Memoirs for the Year 1718, repeats the same Demonstration; except that, before it, he shews, that if several Points be taken upon a Terrestrial Meridian, on the Surface of an Elliptick Earth, as G, H, I, K,\* in such Manner, that their respective Zeniths Z, L. M, N, are diffant from one another, an equal Number of Degrees measur'd in a Celestial Meridian. The Lines ZG, LH, MI, NK (which are perpendicular to the Ellipse) being produced, will meet in the Points O, R, and S, making equal Angles; but as those angular Points are not equally distant from the Curve of the Ellipse. that Elliptic Arc must be the longest whose angular Point is farthest off. Now, by the former Demonstration, it appears, that those Arcs, which are taken nearest to the leffer Axis, will have their angular Points farther remov'd. &c.

If Monf. Cassini's Measures of Terrestrial Degrees, decreasing from the Æquator towards the Pole, were grounded on Observations liable to no Error, he wou'd have fully prov'd his Figure of the Earth. But since those Measures (however accurately taken) are not built upon a mathematical Certainty, his Premises may be call'd in Question, and his Conclusion, tho' mathematically drawn from these Premises, is only probable.

Now therefore, if I can shew from undoubted Phanomena, that his Conclusion will lead to an Absurdity, his Measures must be false; because his Reasoning from them is just. This I shall endeavour to do first, which will disprove his Figure of the Earth; and afterwards endeavour to point out some of the Errors which

I suppose to have occasion'd the Mistake in the Meafures.

Monf. Cassini, as well as the English Astronomers, believes that the Earth makes one Revolution about its Axis, once in 23 Hours 561, because in that Time, the Plane of any Meridian returns to the same fix'd Star

from which it had departed.

Let \* H be taken in any Parallel of Latitude, as for Example, in the Latitude of 51 0 46%, a Plumb Line, L H, will be perpendicular to the Curve BH, at H, and produced pass thro' the Zenith of the Point H. if the Earth had no Diurnal Rotation; but fince the Earth moves round its Axis, all Bodies upon its Surface, endeavour to fly from the Axis of their Motion with a Force proportionable to their Distance from it in a Direction along the Plane of that Parallel, in which they are. Let that Force (explain'd by Monf. Huygens, and called a Centrifugal Force) be represented by the Line H & or its Equal and Parallel L b; now a Plummet placed at L, if the Earth flood still, would descend in the Line LH, but as it is at the same Time acted upon by the Force H 1 in the Direction L b, it will move in the Direction L 1 Diagonal of the Parallelogram H 1, according to the known Laws of Mechanicks; and the Plumb Line LH, instead of being perpendicular to the Curve at H, will in the Latitude 51 0 46' make an Angle of 5' with H L. This Angle will be less towards the Poles, till at the very Pole it quite vanishes, as it also does at the Aquator. The Demonstration of the Quantity of this Angle, I shall give before I end this Differtation. Now fince there is no fuch Angle obfery'd, but in all Water Levels we find the Plumb Line always perpendicular to the Line of Level, the Surface Surface of the Earth must be depress'd towards G, and rise farther from the Axis towards I, in order to become perpendicular (that is, to have its Tangent perpendicular) to the Line L1, in which we have shewn that the Plumb Line must descend.

If there is any Body so fond of Monsieur Cassini's Hypothesis, as to deny the Diurnal Motion of the Earth for the sake of it, I hope they will be convinc'd, when I shew the Measures, upon which it is founded, to be insufficient for determining the different Lengths of the Degrees of a Terrestrial Meridian.

But here I would not be thought to endeavour to lessen the Praise due to the Gentlemen of the Royal Academy, for carrying on a Meridian the whole Length of France, from Dunkerque thro' the Royal Observatory at Paris, quite to the Pyrenæan Mountains on the Borders of Spain. Astronomy and Geography are doubtless much indebted to the Encouragement given by the French Government, and to the Care of their Mathematicians, who have omitted no proper Method for drawing their Meridian, and correcting it as they went on. So many Observations of the rising and fetting Sun, fo many equal Altitudes of the fame Stars accurately taken, fo many Digressions of Stars, so many other Observations made with the Telescope and good Pendulum-Clocks — all compar'd together, for the true fettling of the direct Way of this famous Meridian, leave no Doubt but that it is as perfect as the Nature of the Thing is capable of. And, certainly, by the Help of this Line, and the several Triangles made use of for carrying it on, a better Map of France is made, than has ever been of any Country before: Nay, besides, I believe we may, at a Medium, very well receive their Number of 57060, or 57061 Toises, for the Measure of a Degree of a Meridian of the Earth,

one with another. But to say, that those Gentlemen cou'd observe the Latitude so nicely, as to find a Difference in the Length of the Terrestrial Degrees, and that only of eleven or twelve Toises, (when they made it the least) or of thirty-one Toises, (when they made it the most) is attributing to them an Exactness, so far beyond the Nature of the Instruments which they made use of, that it wou'd be rather a Dispraise than a Commendation to insist upon it.

For in the first Place, the Instrument, with which they took Observations for the Latitude at the two Ends of their Meridian, was a ten Foot Sector (which was worfe than that which Monf. Picard had made Use of before. because the Telescope of his Sector was of ten Foot, whereas Monf. Cassini's was but of three Foot, tho' applied to the ten Foot Sector) where the two hundreth Part of an Inch answers to eight Seconds of a Degree: Now the two hundredth Part of an Inch, being one of the least visible Parts that we can see in a divided Line; they could not take an Angle nearer than that; nay, their Instrument, according to their own Description of it, was divided but to every twenty Seconds. they allow, that fixteen Toises, upon the Surface of the Earth, answer to one Second in the Heavens; and they don't pretend to have taken an Observation nearer than to about three Seconds, which therefore cannot determine a Difference less than forty eight Toiles; whereas the Degrees are only suppored to decrease at most, thirty one Toiles each, from Collioure to Dunkerque. an Error of eight Seconds wou'd make a Difference of one hundred and twenty eight Toises, on the Surface of the Earth; above ten Times greater than the Difference of Degrees in the first Supposition, and four Times greater than that Difference in the last. Besides, the Latitude was not observ'd in the intermediate Places

between Paris, and Collioure, with the abovemention'd Instrument of ten Foot Radius; but they made Use of a Quadrant, whose Radius was only thirty nine Inches, and sometimes an Octant of three Foot Ra-Nay, they fay themselves, in their Account, that it is not the Observations made at the Ends of the Meridian, that we are to deduce the Difference of the Length of a Degree from, but the Altitudes taken at several Places between the Extreams; and, if we grant, that they can take an Angle very well, to four or five Seconds, with the great Instrument, they cannot come nearer than twelve or fifteen Seconds, with the Quadrant or Octant, which we must depend upon for the Difference of the Measure of Degrees: So that upon the whole, we are to determine a Length of thirty one Toises, by an Instrument which is liable to err above two hundred.

If any Consequences of this Kind cou'd be drawn from actual measuring, a Degree of Latitude shou'd be measur'd at the Æquator, and a Degree of Longitude likewise measur'd there; and a Degree very northerly, as for Example, a whole Degree might be actually measur'd upon the Baltick Sea, when frozen, in the Latitude of sixty Degrees. There, according to Mons. Cassini's last Supposition, a Degree wou'd be of 56653 Toises, whereas, at the Æquator, it wou'd be of 58019 Toises, the Difference being 1364 Toises, about the two and fortieth Part of a Degree, which must be sensible; and likewise the Degree of Longitude wou'd, according to him, be of 56817 Toises, less by 1202, or the forty eighth Part, than a Degree of Latitude at the same Place.

But here it may be objected, that the the Latitude was not taken with the ten Foot Sector, in the intermediate Places between *Paris* and *Collioure*, yet the Vol. XXXIII. Hh

Latitude was taken with that Instrument at Dunkerque. Paris, and Collioure, and therefore the fouthern Part of the Meridian, containing 6 ° 18' 56" may be compar'd with the northern Part of it, which contains 2 0 12' 16"; and that the former appears to contain more Toises, in Proportion to the Difference of Latitude at its Extremities, than the latter. To this may be answer'd, that, even in this Case, the Observations made cannot be nice enough to determine the Difference of the Length of Degrees; but there is another Error, which might confiderably mislead the French Gentlemen, and make the Degrees appear longer in the South of France; that is, the Error in taking the true Height of several Mountains in Auvergne, Languedoc, and among the Pyraneans, For if they have allow'd too much for the Air's Refraction (which, by the Observations of Travellers, is greater towards the northern Regions, and diminishes as we go Southward) the Heights of those Mountains will be taken too little, and their Bases confequently longer, which will make the Degrees appear bigger than they are. Let ABCD, \* for Example, be a Mountain, as the Mountain of Rodez, in the Latitude of 44° 21', whose Height BD is 300 Toises, and whose Sides A B and B C (suppos'd to make an Angle of 260 33', with the Horizon) are found by Trigonometry, to be of 670 8 Toiles each; if by a Mistake, in taking the Height, it be suppos'd only equal to ED, or 257 Toises, then the Lines AB and BC will become EF and EG; so that the Base AC, which before was of 1200 Toiles, will become equal to FG, which will appear to be 1279,6 Toises, by Eucl. 47. 1. Now one fuch Mistake, in one Degree, will give a Difference above twice as great as the suppos'd Difference rence of Degrees in that Latitude, which they make of 31 Toises. And that there was a Mistake of this Kind in taking the Height of that Mountain, I shall shew.

The Vapours, that generally float in the Air about the Tops of high Hills, make it so difficult to take their Height exactly, that Experiments, made with the Barometer, will, by observing the Fall of the Mercury, shew the Height nearer than any Thing else we know of. There were, indeed, several Experiments made with the Barometer, where the Differences of the Height of the Mercury, from the Heights at which it stood at the Royal Observatory, are said to answer to so many Toises; but of nine Observations mention'd by Mons. Cassini, there are not two where the Number of Toises, said to correspond to the Heights of the Barometer, do agree together.

The first Experiment of the Barometer there mention'd, made at Collicure, was this, "At the Height of 11½ Toises above the Sea, the Barometer was set up, and the Mercury stood 3½ Lines higher than at the Royal Observatory (in the Tower of the eastern Hall) at the same Time; and therefore, since that Tower is 44 Toises higher than the Sea, 3½ Lines

of Mercury must answer to 321 Toises.

Now, reducing these Toises to Feet, and dividing by 3; it will appear that an Height of 58,5 Feet will answer to the Fall of one Line of Mercury in the Barometer. Let this be taken as the Standard, and the other Observations be compar'd with it. This may be done by the following Table, where the first Column shews the Place where the Observation was made; the second, the Fall or Rise of Mercury at each Place express'd in Lines, or 12th Parts of a French Inch; the H h 2 third.

<sup>\*</sup> Mem. of the Royal Academy, for 1718, ch. 10.

third, the Heights or Depths answering to those Lines of Mercury, which, in the Memoirs, are given in Toises, but here reduced to Feet; the sourth, the Number of Feet answering to one Line of Mercury in each Observation, which is the Quotient of the Feet in the third Column, divided by the Number of Lines in the Second.

Observations of the Ba <sup>ro</sup> - meter made at	Lines of Mercury.	Said to corre- fpond with Feet.	The Fall of one Line of Mercury and fwers to Feet,
I. Collioure	03 2	1.95	58,5
II. The Tower of Massane.	31	2382	76,8
III. Bugarac -	42	3636	86,5
IV. Rupeyroux	30	2181	72,7
V. Rodez	24	1647	68,6
VI. Rodez -	20	1425	71,25
VII. Courlande -	5:4	4812	89,1
VIII. Coste	54	4890	92,4
IX. Clermont	0.3	200	66,6

A Sight of this Table will convince any one, that these Observations are not to be depended upon for determining the Height of the Mountains in the South of France; for the Differences are not small, such as might happen in making the Experiments; but fuch as render the Observations useless for the Purposes abovemention'd. For Example, the first and the seventh differ almost :: And if 58;5 Feet were allow'd for the Fall of one Line of Mercury in the feventh Observation. instead of 944 Feet, then the Mountain of Coste would be but 3.085 Feet, instead of 4890. Nay, upon examining the Memoirs, I find that in feveral Observations the Number of Toises, said to correspond to a certain Height of Mercury, are only answerable to the Height of the Mountain above the Level of the Sea found by Trigonometry, from which the Height of the Royal Observatory, above the Sea, is substracted; though, by the Manner of the Expression, a cursory Reader would imagine imagine, that the Number of Toises nam'd, was always proportionable to the Fall of the *Mercury*, and think all the Experiments and Observations very accurately made, when they seem to agree so well in every Respect.

Now after all, I do not question but that the Height of the Barometer, might be as it is set down in the Memoirs, and well enough observed; but it was wrong to compare the Height of the Mercury in the South of France, with the Height that the Mercury was at in the Barometer of the Royal Observatory at the same Time; for, at that great Distance and Difference of Latitude, the Weather (and consequently the Pressure of the Air and Height of the Barometer at the same Level) might very much vary.

Even when there is fair Weather all over France, it does not follow that the Barometer shall stand at the same Height: Let us suppose, for Example, that a North Wind blows: Where ever the Air is check'd by a Chain of Mountains that run East and West, it will be accumulated over those Mountains, and consequently press more as its Columns are higher; which will make the Mercury rise higher than it wou'd do with the same Wind, if there were no Mountains, or if they ran North and South.

The Way, to have made the Experiments with the Barometer exactly, wou'd have been to have observed the Height of the Mercury at the Bottom and at the Top of the Mountain, and that with a Tube of a pretty large Bore (with a proportionably large Cistern for the stagnant Mercury) because, in a small Tube, the Mercury will often stick to the Sides, and rise irregularly, as it will also in inclin'd Barometers. Simple Barometers are the best, and a magnifying Glass may be made use

of to observe small Rises or Falls, having two fine and well made Indices to the Tube.

Dr. Edmund Halley, our Royal Astronomer, has, fome Years ago, given us, in the Philosophical Transactions, the Falls of Mercury in the Barometer. corresponding with the Heights to which the Barometer must be carried to produce those Falls. The first tenth Part of an Inch in the Fall of the Mercury, he makes to answer to an Height of 90 Feet; the next tenth, to an Height something greater, and so in Proportion, as the Air diminishes in Density, according as we rise in Height. The Proportion of the first Tenth of the Mercury's Fall, he has built upon the Comparison of the different Specifick Gravities of Air and Mercury: and taking Mercury to be 13½ Times heavier than Water, and Water (in cold Weather) to be 800 Times heavier than Air; it follows, that 13,5 × 800, will give 10800; which Number, if it be taken in Feet, and divided by 120 (the Number of the 10th of an Inch in a Foot) we shall have 90 Feet answerable to the 10th of an Inch, and 75 Feet to a Line or the 12th Part of an Inch. As the Doctor's Tables may be of use to the Curious, I have inferted them here.

## I. A TABLE shewing the Attitude, to given Heights of the Mercury.

Inches. 30	Ó	Feet.
29	915	
28	1862	
27	2844	
26	3863	
25	4922	
20	10947	
15	18715	
10	29662	
5	48378	
I	91831	
0.5	110547	
0.25	129262	
O. I	29 Miles or 154000	
0.01	41 Miles or 216169	
0.001	53 Miles or 278338	

II. A T A B L E shewing the Heights of the Mercury, at given Altitudes.

Feet. o	30	00	Inches and Tenths.
1000	28	91	
2000	27	86	
3000	26		
4000	25	87	
5000	24	93	
r Mile	24	67	
2	20	29	
3	16	68	
4 5	13	72	
5	11	28	
10	4	24	
15	1	60	
20	0	.95	
25	O	23	
30	0	08	
40	0	012	

Now, as very few Mountains in the World are 3 Miles high, and, generally speaking, those that we look upon as high Hills, (except the Andes, and some others in America) are not much above a Mile high; we may, for finding the Height of Mountains, take a fix'd Number of Feet in Altitude to answer to every 10th or 12th of an Inch in the Fall of the Mercury; because 90 Feet are by Dr. Halley only taken for the first Tenth, and greater Heights for other Tenths, encreasing with the Fall of the *Mercury*. Therefore I wou'd propose another for a round Number, namely 96 Feet for every Tenth, and 80 Feet for every 12th of an Inch, very near the Number that I have found by my Calculation, which is as follows. Fine

Fine Mercury (such as is made use of in Barometers) is, generally speaking, 132 times heavier than Water: and, I found some brought from the East-Indies, to be 14 times heavier. I have found Air in Summer. to be near 900 times lighter than Water; and 800 times in Winter; therefore I take 850 at a Medium. Now 850  $\times 13^{\frac{1}{3}} = 11606,6$ , which, divided by 120, gives 96.7 Feet, for to of an Inch of Mercury, or 80.5 Feet for it of an Inch. This Number, taken invariable, will, in taking the Height of feveral Hills, agree pretty well with the Numbers that come out, when Dr. Halley's Table is made use of; and with the Experiment made by the late Professor, Mr. J. Caswell, who, having taken the Height of Snowdon Hill in Caernarvanshire very accurately, and finding it to be 3720 Feet above the Level of the Sea, tried how much lower the Mercury wou'd stand in the Barometer upon that Hill, than at the Level of the Sea, and observ'd it to subside 3 9 Inches. I am sensible that it will be alledged, that the Air will be denser than I may imagine on the Top of high Hills, because of the great Cold, since they are generally cover'd with Snow; but then we are to confider, that when we are got above a Mile higher than the Level of the Sea, the incumbent Atmosphere has lost almost a 5th Part of its Weight \*; and therefore the Air at the Top of the Hill, being so much less press'd, will, notwithstanding the intense Cold, be more rarified than at the Bottom of the Hill.

<sup>\*</sup> If the whole Air was reduced to the same Density, as it is near the Level of the Sea, the Atmosphere wou'd be but between five and six Miles high; whereas, in its present State of gradual Rarefaction, it is above 50 Miles high, as we find by several Phænomena of Meteors observed to float in the Air, so high at least.

Now if we go back to the Observations of the Barometer, made by the Gentlemen that drew the Meridian in France, we shall find, that on the Mountain of Rhodez, in the Latitude of 44°, 21' the Barometer fell 24 Lines below the Level of that in the Observatory. and they allow'd only 2742 Toises to correspond to that Fall; whereas, according to Dr. Halley's Proportion of a Tenth of an Inch for 90 Feet, they shou'd have taken 300 Toises; and the Hypotenuses AB, and BC, \* were taken longer than the bare Declivity of the Mountain (which wou'd make the Error lefs than the 79 Toises I mention'd above) yet if my Proportion be made use of, viz. of 80 Feet for each Line of Mercury, that will make the Mountain 320 Toises, which, being higher, will therefore shew the Base to be yet fhorter, and confequently the Error, at that Rate, will be greater.

This Error (and fuch like, if any more were made) will encrease the Measure of the 44th Degree of Latitude on the Earth; and, by observing what was done in the next Degree, we shall find that that Degree was taken too short. In the Latitude of 45°, 381, the Mountain of Coste is made 815 Toises high; whereas the 54 Lines of the falling Mercury in the Barometer, faid to answer to that Height, will give but 705,6 Toifes (which we will call 705,5) even according to my Computation of 80 Feet to a Line, which is the greatest Allowance. If we suppose this Mountain to rise in an Angle of 26°, 33', as we did that of Rhodez, the Sides of the Mountain, or Hypotenuses AB, and BC, † will be each equal to 1577,54 Toifes, and the whole Base A C, to 2822 Toises. Now, when the Height of this Mountain is call'd 815 Toifes, the Base AD, or DC

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(by Eucl. 47. 1.) becomes only equal to FD or DG = 1350,7 Toises, and its Double, or FG the whole Base, will be but 2701,4 Toises, less than the former by 120 6 Toifes. This Error is fo great (so much more than the Difference of 31 Toises for a Degree) that tho' Isuppos'd the Lines found by Trigonometry, which terminate at the Top of the Mountain, to be much longer than the Hypotenuse A B, yet there will be Error enough to make the 45th Degree of Latitude appear much shorter than Supposing (because of the Length of the Lines AB, or the great Distance from which the Mountain might be observ'd) that these Errors were four times less than I made them; yet, at that Rate, one must add near 20 Toises to the 44th Degree of Latitude, and take away above 30 from the 45th Degree, which will make the 44th of 57080 Toises, and the 45th, of only 57030; and this will give a Difference of 50 Toises; so that if an Angle can be taken to two or three Seconds, to which 32, or 48 Toises, are said to answer upon the Surface of the Earth, such a Difference might be visible.—And much more so, if other Errors of the same Kind shou'd happen to have been made the same Way; or if those Errors were nearer my first Supposition than this last. Nay, tho' the 45th Degree of Latitude may be 13 Toises bigger than the 44th, it might by this Means appear to be confiderably less-

Such a Mistake might be the Occasion of making the Hypothesis of the Earth being an oblong Spheroid, especially because in this Hypothesis, the Degrees differ most in Length from one another about the 45th Degree; and, when once an Hypothesis is set on Foot, we are too apt to draw in Circumstances to confirm it; tho, perhaps, when examin'd impartially, they may rather weaken, than strengthen our Hypothesis; otherwise, the Author of the History of the Royal Academy, for the

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Year

Cassini observ'd Jupiter to be oval, as a Proof of young Mons. Cassini's Hypothesis; because Jupiter is oval the other Way, that is, an oblate Spheroid flatted at the Poles, as the said late Mons. Cassini gave the Proportion of the Axis, to the Æquatorial Diameter, to be as 13 to 16.——— And our late ingenious Astronomer, the Reverend Mr. Pound, with a Telescope of 123 Foot Focus, and an excellent Micrometer, has given those Proportions as 11 to 12. If a Proof is to be drawn from Analogy, or what is observ'd in other Planets, this must destroy Mons. Cassini's Hypothesis, and consirm Sir Isaac Newton's.

The Opinion of Dr. Burnet (the Theorist) quoted in the Memoirs, for the Year 1713, is but a very weak Argument in favour of Mons. Cassini's Hypothesis, on Account of the Reason Dr. Burnet gave, to prove the Earth higher at the Poles, than the Æquator; for he says, "That the Velocity of the Parts of the Earth, in its Diurnal Rotation, being greater at the Æquator tor than towards the Poles, all the Water must be driven towards the Aquatorial Regions; from whence, being repelled by the Resistance of the Air, it must run off again towards the Poles; and fo the Figure of the Water was lengthen'd out into an oblong Spheroid, and consequently the Crust of the Earth over it did put on the same Figure, &c.

But why the Air shou'd resist more towards the Æquator than the Poles, the Doctor did not give any Reason to shew; and, if it had been so, the same Force, that drove the Water towards the Æquator, must have kept it there. The Doctor, in the latter Part of his Assertion, forgot what he had said in the former; for the Water cou'd not run off towards the Poles, whilst the Earth continued its Rotation with the same Velocity.

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For if he had consider'd, he wou'd have sound his Argument in other Words to be this. Because Bodies, that move in a Circle, always endeavour to recede from the Axis of their Motion; therefore the Water, by that Endeavour, comes nearer to the Axis of its Motion; which is absurd. But Dr. Burnet, afterwards, alter'd his Opinion, as I am credibly inform'd.

Having thus given my Reasons for disapproving of Monf. Callini's Opinion, concerning the Figure of the Earth; I come now to consider Sir Isaac Newton's, who makes it higher at the Aguator, than at the Poles; but before I enter upon it, I beg Le we to quote a Para. ragraph out of the History of the Royal Academy for 1713. These are the Words of the Author. "Reafonings drawn from the different Lengths of a Pen-" dulum in different Climates, or from the Inequality " of the Centrifugal Force arising from the Diurnal Motion of the Earth, are, perhaps, too nice to pro-" duce a certain Conviction; nay, perhaps, we are not " well enough affured of the Principles, and the Consequences may sometimes be different. And " therefore it is evident, that the best Way in this En-" quiry, is only (as Monf. Caffini does) to make use " of unquestion'd Observations, which serve directly " to decide the Question.

That Mons. Cassini has not made use of unquestion'd Observations, and the Measures, he mentions, are not able to decide the Question, appears from what I have already said. We must therefore shew, whether the Principles, from which Sir Isaac Newton has deduced his Figure of the Earth, are fully prov'd or not: Whether the Conclusion drawn from them is plain and evident; and whether the Experiments on Pendulums, that confirm the Theory, are easy to be made, and may be depended upon.

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Tho' Sir Isaac Newton, in his Principia, has not endeavour'd to give the Cause of Gravity, or to determine whether it be owing to an Impulse or not; yet he has shewn what its Effects and Laws are, from plain Experiments made by others and himself. From the Laws of Gravity, and from the Observation of a Comet, \* he has deduced the Annual Motion of the Earth; and it must have a Diurnal Motion, if it has an Annual one, otherwise, it will not agree with the Phanomena. The Laws of the Centrifugal Force, or that Force by which a Body, whirl'd round in any Circle, endeavours to recede from the Center of its Motion, have been demonstrated by Mons. Huygens.

These are the Principles from which Sir Isaac Newton draws his Conclusion; and the some Persons, that will not be at the Pains to examine them, may deny them by the Lump, yet no Body has yet been able to shew any Flaw in the Demonstrations that relate to

them.

NB. This Dissertation will be continued in our next.

<sup>\*</sup> Princip. Lib. 3. Prop. 12, 13, & 42.